IMAGE SUPER-RESOLUTION USING MULTI-LAYER SUPPORT VECTOR REGRESSION

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ABSTRACT
Existing support vector regression (SVR) based image super-resolution (SR) methods always utilize single layer SVR model to reconstruct source image, which are incapable of restoring the details and reduce the reconstruction quality. In this paper, we present a novel image SR approach, where a multi-layer SVR model is adopted to describe the relationship between the low resolution (LR) image patches and the corresponding high resolution (HR) ones. Besides, considering the diverse content in the image, we introduce pixel-wise classification to divide pixels into different classes, such as horizontal edges, vertical edges and smooth areas, which is more conducive to highlight the local characteristics of the image. Moreover, the input elements to each SVR model are weighted respectively according to their corresponding output pixel’s space positions in the HR image. Experimental results show that, compared with several other learning-based SR algorithms, our method gains high-quality performance.

Index Terms— Super-resolution (SR), support vector regression (SVR), multilayer, pixel-wise classification

1. INTRODUCTION
Image super-resolution (SR) technique is to simulate the process of image degradation of imaging system (optical blur, motion blur, undersampling and system noise, etc), and to generate a raster image with a higher resolution than its source [1]. The existing SR methods can be roughly divided into three categories: interpolation-based, reconstruction-based, and learning-based. Recently, learning-based SR methods have attracted ever-increasingly attention due to its ability to restore high frequency details in texture areas with the help of other example images. The essence of these methods is to establish a model between low-resolution (LR) image and its corresponding high-resolution (HR) one, and then to estimate the model parameters using the training set. However, these methods suffer from serious boundary effect, for the reason that they only construct the mapping relationship from LR patches to HR patches.

To solve the boundary effect occurred in learning-based SR techniques, some investigations on the application of SVR to SR problem are conducted from different perspectives. Ni et al. [2] proposed an SVR-based SR method, which takes the LR image patches removed the center pixel as input and the corresponding HR image patches as output, respectively. Unfortunately, this method ignored the significant role of the center pixel in the LR image patch. Along this way, Li et al. [3] adopted the interpolated image patches as input and the center pixel of corresponding error image (i.e., the difference between the original image and the interpolated one) patches as output. Although this method attempted to build a mapping between patch and pixel instead of between patch and patch to overcoming boundary effect, it makes the resulting image over-smoothing.

In this paper, we propose a multi-layer SVR based SR algorithm to address the aforementioned issue. We use SVR to model the relationships not only between LR image to its corresponding HR one, but also between LR image and the error image (i.e., the difference between pseudo high-frequency image and the original image), by extending single layer SVR model to a multi-layer model. Due to the fact that training SVR model in the whole image directly may not consider the diverse content in the image, we introduce pixel-wise classification to divide pixels into horizontal edges, vertical edges and smooth areas for training. Moreover, we weight the input set of each SVR model according to the space position of its corresponding pixels in the HR image patches, respectively.

The remainder of this paper is organized as follows. Section 2 introduces support vector regression. Then we describe our algorithm and analyze our model for imaging systems in Section 3. Experimental results are given in Section 4. Section 5 concludes this paper.

2. SUPPORT VECTOR REGRESSION
Support vector regression (SVR) machine is an application of support vector in the field of regression function [4]. The SVR classification is that the sample points only have one category which seeks the optimal hyperplane not to make two types of sample points share the “maximum margin”, but to make all the sample points smallest away from the “total deviation”. While the sample points are between two boundaries,
seeking the optimal solution, the hyperplane that maximizes the margin [5].

2.1. SVR Model

In linear case, SVM fitting function first considers a linear regression function \( f(x) = \omega \cdot x + b \) to fit \((x_i, y_i)\), \(i = 1, 2, ..., n\), where \(x_i \in \mathbb{R}^n\) is input and \(y_i \in \mathbb{R}\) is output. That is, we need to determine \(\omega\) and \(b\).

Penalty function is a measure of error in model learning process, generally selected before learning. Different learning problems correspond to different loss functions. Standard support vector machine adopts \(\epsilon\)-nonsensitivity function, that is, with an assumption that all the training data are fitted by a linear function under \(\epsilon\)-accuracy

\[
\begin{align*}
    y_i - f(x_i) & \leq \epsilon + \xi_i \\
    f(x_i) - y_i & \leq \epsilon + \xi_i^* \quad i = 1, 2, ..., n
\end{align*}
\]

where \(\xi, \xi^*\) are relaxation factors.

In this case, the problem is transformed into an object function minimization problem

\[
R(\omega, \xi, \xi^*) = \frac{1}{2} \omega \cdot \omega + C \sum_{i=1}^{n} (\xi_i + \xi_i^*)
\]

where the first term is to make the fitting function smoother and to enhance the generalization capability; the second term is to reduce error; and the constant \(C\) expresses the degree of punishment for the samples that exceed the error \(\epsilon\).

2.2. \(\epsilon\)-Support Vector Regression (\(\epsilon\)-SVR)

The basic idea of a nonlinear SVR model is to map the input vectors into a high-dimensional feature space (Hilbert space) using a predetermined nonlinear mapping, and to do linear regression in the space.

First we map the input \(x\) into the high-dimensional feature space \(\Phi\) through the mapping \(\phi : \mathbb{R}^n \rightarrow \Phi\), and adopt \(f(x) = \omega \cdot \phi(x) + b\) to fit data \((x_i, y_i), i = 1, 2, ..., n\). Consider a set of training points, \(\{(x_1, z_1), (x_l, z_l)\}\), where \(x_i \in \mathbb{R}^n\) is a feature vector and \(z_i \in \mathbb{R}\) is the target output. For parameters \(C > 0\) and \(\epsilon > 0\), the standard form of support vector regression [6] is

\[
\begin{align*}
    \min_{\omega, b, c, \xi, \xi^*} & \quad \frac{1}{2} \omega^\top \omega + C \sum_{i=1}^{l} (\xi_i + \xi_i^*) \\
\text{subject to} & \quad w \cdot \phi(x_i) + b - z_i \leq \epsilon + \xi_i \\
& \quad z_i - w \cdot \phi(x_i) - b \leq \epsilon + \xi_i^* \\
& \quad \xi_i, \xi_i^* \geq 0, i = 1, ..., l
\end{align*}
\]

The dual problem is

\[
\begin{align*}
    \min_{\alpha, \alpha^*} & \quad \frac{1}{2} (\alpha - \alpha^*)^\top Q (\alpha - \alpha^*) \\
& \quad + \epsilon \sum_{i=1}^{l} (\alpha_i + \alpha_i^*) + \sum_{i=1}^{l} z_i (\alpha_i - \alpha_i^*) \\
\text{subject to} & \quad e^\top (\alpha - \alpha^*) = 0, \\
& \quad 0 \leq \alpha_i, \alpha_i^* \leq C, i = 1, ..., l
\end{align*}
\]

where \(Q_{ij} = K(x_i, x_j) \equiv \phi(x_i) \cdot \phi(x_j)\), \(\phi\) is unknown and high-dimensional. Support vector machine theories only consider the dot product \(K(x_i, x_j)\) as \(\phi(x_i) \cdot \phi(x_j)\) called kernel function in high-dimensional feature space and do not use function \(\phi\) directly.

After solving the problem above, the approximate function is

\[
\sum_{i=1}^{l} (\alpha_i + \alpha_i^*) K(x_i, x) + b
\]

In LIBSVM, we output \((\alpha - \alpha^*)\) in the model.

3. SVR BASED SUPER-RESOLUTION

With the support vector regression and its solving method, we discuss how to apply SVR to image super-resolution in this section.
super-resolution, as shown in Fig. 1, by a factor of $I$. Responding to the center pixel. For instance, in the case of $W$, the error image model is $I$. Suppose that the reconstructed image using one layer of SVR is $I_{LR}$ and $I_{HR}$ image patches areas for training. Then, we do the same in each part. Given $I_{LR}$, the original HR image $I_{HR}$ can be expressed as $I_{HR} = I_{LR} + e$, where $e$ is the difference between $I_{LR}$ and $I_{HR}$.

This is a multi-output regression problem [7], which can be solved directly or be divided into several separate single output regression problems according to the current literature [8]. Here we adopt the second method, treating the multi-output regression problem as several separate single output regressions. Therefore, learning the four outputs becomes $\{g^{(j)} = g^{(j)}(x)\} \subset \mathbb{R}$ for $j = 1, ..., 4$, given the input $x \in \mathbb{R}^{N^2}$, and $g^{(j)}$ is estimated by $c$-SVR in Eq. (4). To further improve the results, a multi-layer SVR model is proposed.

3.2. Multi-layer SVR Model

Suppose that the reconstructed image using one layer of SVR model is $\hat{I}_1$, the original HR image $I_h$ can be expressed as

$$I_h = \hat{I}_1 + I_e$$

where $I_e$ is the difference between $I_h$ and $\hat{I}_1$.

Introducing the second level SVR model is to reconstruct the error image $\hat{I}_{e_1}$, and to make it as close as possible to $I_e$.

$$I_e = \hat{I}_{e_1} + I_{e_2}$$

where $I_{e_2}$ is the difference between $I_e$ and $\hat{I}_{e_1}$.

Introducing the third level SVR model is to reconstruct the error image $I_{e_2}$, and to make it as close as possible to $\hat{I}_{e_2}$, as shown in Fig. 1. By analogy, if we adopt $N$ layers SVR model, we can obtain the final constructed results as follows:

$$I_h = \hat{I}_1 + \hat{I}_{e_1} + \hat{I}_{e_2} + \ldots + \hat{I}_{e_{N-1}}$$

4. EXPERIMENTS

In experimental parameter settings, we utilize LIBSVM [4], a software package for SVM pattern recognition and regression, to train SVR models. We empirically choose Radial Basis Function (RBF) as the kernel function, setting the parameter $g = 5$ and $c = 1$, and choose $c$-SVR model. $W$ is empirically selected according to the relative position of the pixels. Considering the tradeoff between computation cost and reconstruction result, we choose three layers of SVR model.

We compare our method with several representative learning-based SR algorithms, including the sparse representation based algorithm (ScSR) [9] and the neighborhood embedding algorithm (NE) [10]. The results of those two algorithms are obtained by running the corresponding code packages. All test images are from ASDS-AR [11] algorithm code package. The proposed algorithm uses one of the test images as training image. Here, we use the image girl to train a multi-layer SVR model. To reduce training time and select different types of points, we select a point every ten points, rather than select all points in the training image.

Fig. 3 and Fig. 4 show the comparison of the proposed algorithm and several other representative algorithms. We see that the reconstructed HR images by method [9] have many jaggy and ringing artifacts. The NE algorithm [10] is effective in suppressing the ringing artifacts, but it generates pixel-wise constant block artifacts. The results of the proposed method is best in visual quality. The reconstructed edges are much sharper than all the other four competing methods, and more image fine structures are recovered.

The PSNR and SSIM values of the reconstructed HR images are shown in Table 1. Although the performance differences among these methods are small, we can still observe
Table 1. The PSNR (dB) and SSIM results (luminance components) of reconstructed HR images.

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Fig. 3. Reconstructed HR images of Parrots by different methods. Top row: Original, Bicubic, SCSR. Bottom row: NE, SVR (\(N = 1\)), proposed (\(N = 3\)).

Fig. 4. Reconstructed HR images of flower by different methods. Top row: Original, Bicubic, SCSR. Bottom row: NE, SVR (\(N = 1\)), proposed (\(N = 3\)).

that the proposed method constantly outperforms the competing methods. Also, our multi-layer SVR model can be processed offline and be called during the test process, which greatly reduce the computation cost.

5. CONCLUSION

In this paper, we propose a novel image SR approach based on multi-layer SVR model to restore as much detailed information as possible by building different mapping relationships. Specifically, it constructs the SVR model not only between LR and HR images, but also between the LR image and the error image. Pixel-wise classification is introduced to divide pixels into different classes such as horizontal edges, vertical edges and smooth areas, which is more conducive to highlight the local characteristics of the image. Moreover, the input elements of SVR model are weighed respectively on the basis of the space position of corresponding pixel in the HR image patch. Comparison with existing algorithms shows the advantages of the proposed method.

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7. REFERENCES


