USING A* FOR THE PARALLELIZATION OF SPEECH RECOGNITION SYSTEMS

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ABSTRACT
The speed of modern processors has remained constant over the last few years but the integration capacity continues to follow Moore’s law and thus, to be scalable, applications must be parallelized. This paper presents results in using the A* search algorithm in a large vocabulary speech recognition parallel system. This algorithm allows better parallelization over the Viterbi algorithm. First experiments with a “unigram approximation” heuristic resulted in approximately 8.7 times less states being explored compared to our classical Viterbi decoder. The multi-thread implementation of the A* decoder led to a speed-up factor of 3 over its sequential counterpart.

Index Terms— Speech recognition, A*, parallelization

1. INTRODUCTION

Large vocabulary automatic speech-recognition is a computationally intensive task. Most speech recognizers run under a sequential implementation that cannot take advantage of modern processors with multi-core technology. In order to exploit this power, a parallel speech recognition system must be implemented.

The two major time consuming components are the acoustic likelihood computation and the optimal path search. The first component takes 30\%-70\% of total time. This calculation involves mostly arithmetic operations than can be computed by a dot product. This allows an efficient implementation in a SIMD (Single Instruction Multiple Data) parallel architecture such as SSE registers or a graphic processor (GPU) [1].

The search component consumes most of the remaining time. The classic way to perform the decoding uses the Viterbi algorithm. This algorithm is simple and straightforward to implement. It is nonetheless difficult to achieve an efficient parallelized version of the Viterbi algorithm on a classical multicore computer. The main reason is that only 1\% of the states are active at each frame and these are scattered in memory. This situation adds to the well established difficulty of having to search a sparse graph on a parallel architecture of the Intel processor type [2].

A parallel implementation of a speech recognition system is presented by Phillips et al. [3]. Their system builds the transducer on the fly during the decoding process. They have obtained a performance of 0.8x real-time on a 16 CPU computer for the North American Business News (NAB) database. This is a speed-up of 4.87 compared to 3.8x real-time on a single CPU.

Parihar et al. implement the parallelization of the search component of a lexical-tree based speech recognizer [4]. In this work, lexical-tree copies are dynamically distributed among the cores to ensure a good load balancing. This results in a speed-up of 2.09 over a serialized version on a Core i7 quad (4 cores) processor. The speed-up is limited by the memory architecture.

In [5], Ishikawa et al. implemented a parallel speech recognition system in a cellphone using a 3-core processor. The system was divided in 3 steps, one for each core. They reported a speed-up factor of 2.6 but their approach is not scalable since involved steps are not easily parallelizable.

This paper presents results of using the A* search algorithm in a large vocabulary speech recognition parallel system. This approach has previously been applied to speech recognition by [7]. It divides the search operation into two steps. The first step is the computation of a heuristic that yields an estimate of the cost for reaching the final state from any given state in the graph. The second step is a best-first search driven by the heuristic. The advantage of this approach is that the heuristic can be constructed to allow an efficient computation in parallel. The search itself is still difficult to parallelize, but it can be reduced by using a good heuristic since, in this case, a smaller number of states will be explored.

This paper is organized as follows. Section 2 presents the A* algorithm and how it is used in the context of speech recognition. Section 3 presents preliminary experimental results obtained on a large vocabulary speech recognition task.

2. A* DECODER

Unlike the time synchronous Viterbi algorithm, the A* algorithm is a best-first scheme, that implies a scoring procedure to explore the most promising states. The score of a state is

\[ \text{Score}(q) = g(q, t) + h(q', t + 1) + \text{cost}(q, q') \]
where \( g(q, t) \) is the score for reaching state \( q \) from the initial one at time \( t \), \( h \) is the heuristic score that gives an estimation of the cost for reaching a final state from the adjacent state \( q' \) at time \( t + 1 \) and \( \text{cost}(q, q') \) is the cost for going to \( q' \) from \( q \). A heuristic is said to be admissible if, for every state, it underestimates the real cost for reaching the final state. In that case, the A* algorithm is optimal. A pseudocode of the A* algorithm is shown in Algorithm 1.

The input of the algorithm is the HCLG recognition network composed of HMMs (H), triphone context dependency (C), lexicon (L) and a trigram backoff language model (G). This network is represented by a \( \text{WFST} = (Q, \Sigma, \Xi, \delta, \Omega) \) where \( Q \) is a set of states, \( i \in Q \) is the initial state, \( F \subseteq Q \) is the set of final states, \( \Sigma_i \) is the input alphabet of the automaton (distributions), \( \Omega \) is the output alphabet of the automaton (words), \( E \subseteq Q \times \sum \times \sum \times \mathbb{R} \times Q \) is the set of transitions, \( \lambda : i \rightarrow \mathbb{R} \) is the initial weight function and \( p : F \rightarrow K \) is the final weight function.

The second input is the heuristic function \( h : q, t \rightarrow \mathbb{R} \) which gives the estimated cost for reaching a final state from state \( q \) at time \( t \).

Algorithm 1: The A* algorithm

```
1 openList ← \{((i, \lambda, 0), \text{heuristic}(i, 0))\}
2 closedList ← ∅
3 while openList ≠ ∅ do
4     /\ Extract state with lowest score
5     (q, t, g) ← openList.Extract()
6     closedList ← closedList ∪ (q, t)
7     if q ∈ F and t = numFrames then
8         // Best path found
9         ExitSearch()
10    end
11 foreach (q, \sigma, \sigma, w, q') ∈ E[q] do
12     if \( (q', t + 1) \) \notin closedList then
13         g' ← g + \text{obsCost}(\sigma, t) + w
14         h ← \text{heuristic}(q', t + 1)
15         entry ← (q', t + 1, g')
16         score ← g' + h
17         openList ← openList ∪ \{(entry, score)\}
18    end
19 end
```

2.1. Unigram Language Model Heuristic

In our implementation, the heuristic is also represented by a WFST. The heuristic costs are computed by performing backward Viterbi decoding. The heuristic FST must be small enough to allow for an exhaustive search. In our experiments, it is built with the same models as that of the recognition network, with the exception that the trigram language model is replaced by a unigram model derived from the trigram. The resulting FST is small enough to be exhaustively and efficiently decoded.

Note that application of the Viterbi algorithm on the heuristic is simpler and faster than on the recognition network because no backpointers need to be kept to retrace the best state sequence. Moreover, since all states are explored at each frame, they reside in contiguous memory locations for optimal cache usage.

2.2. Mapping Recognition FST States to Heuristic States

Recall that A* search uses the heuristic cost given by the function \( \text{h}(q_r, t) \), where \( q_r \) is a recognition FST state. In essence, this function performs a lookup in the Viterbi treillis computed on the heuristic. Thus, we need to know which state \( (q_h, t) \) in the heuristic is equivalent to \( (q_r, t) \). A mapping between states of the heuristic and those of the recognition FST must thus be discovered.

To establish this mapping, we can use the FST composition as described by Mohri [8]. The inverted (input and output symbols swapped) heuristic FST is composed with the recognition FST. A state in the composed FST is a pair \( (q_h, q_r) \) where \( q_h \) and \( q_r \) are, respectively, states of the heuristic and recognition FST. The existence of a state \( (q_h, q_r) \) implies that at least one path from \( i_h \) to \( q_h \) in the heuristic FST has the same distribution sequence than a path from \( i_r \) to \( q_r \) in the recognition FST. Since the composed FST is connected, there is also a path from \( q_h \) to a final state of the heuristic FST that has the same distribution sequence than a path from \( q_r \) to a final state of the recognition FST. Consequently, both states are considered to be equivalent. Note that the FST resulting from the composition is not used, only the list of state pairs is useful. In addition, this mapping is computed offline.

2.3. Block Processing

Data structures required for implementing A* are more complex than the simple array used in a Viterbi decoder. The A* algorithm always explores the most promising path first. For efficiency, paths are stored in a binary heap for which the three main operations (insertion, extraction and decrease key) are in \( O(\log n) \). However, the algorithm needs to know if a node is already in the heap before inserting it. Since searching a node in a heap is \( O(n) \), a hash table is used to keep track of nodes in the open list. Moreover, since we don’t want to explore the same node more than one time, we use a closed list of nodes already explored which is also implemented with a hash table. For efficiency, there is an open list (hash table) and a closed list per frame.

In addition to complex data structures, the number of nodes to explore grows as the square of the number of frames as is the case with the Viterbi algorithm. To circumvent both problems, a block approach has been implemented as follows.
The heuristic is first computed for $\Delta$ frames. Then, the $A^*$ search is performed on the $\Lambda < \Delta$ first frames. The search stops when a node at time $\Lambda$ with a cost (path cost + heuristic cost) larger than the best cost added to a user value (beam) is extracted from the open List.

The window is then advanced of $\Lambda$ frames. The process is applied until the end of audio is reached. In order to save computation time, several consecutive searches can be done with one heuristic computation as shown by Figure 1.

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3. EXPERIMENTATION

3.1. Experimental Setup

The baseline system for comparison is a FST-based speech recognition system developed at CRIM and tuned for speaker-independent transcription of broadcast news.

The acoustic model has been trained with 171 hours coming from French television programs in Quebec. The programs are a mix of weather, news, talk shows, etc. that have been transcribed manually. The acoustic parameters consist of 12 MFCCs plus the energy component, corresponding first and second derivatives, for a total of 39 features. The model contains 4600 distributions of 32 and 128 Gaussians with diagonal covariance matrices.

The language model has been trained with text from a French local newspaper (La Presse, 93 million words) and the acoustic training set’s textual transcripts (2.1 million words). Both the unigram and trigram language models use the same vocabulary of 59624 words.

The CPU used is an Intel Core i7 quad at 2.9 GHz with 8 GB of RAM. Acoustic computations use the SSE registers. On the baseline version, required acoustic likelihoods are computed on-demand. This optimization is not possible with the $A^*$ algorithm since all likelihoods are needed for the heuristic. The heuristic computation itself accounts for 27% of the total time.

For all experiments involving the $A^*$ algorithms, the heuristic length $\Delta$ has been set to 500 frames. $A^*$ search is performed on $\Lambda = 20$ frames with a lookahead of 100 frames. Thus, for each block of heuristic scores, 20 $A^*$ searches are performed.

The test set is made up of 44 minutes (2625 seconds) of audio with a duration between 32 and 50 seconds.

### Table 1. Viterbi vs $A^*$ at real time.

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Computation time (seconds)</th>
<th># of explored nodes</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Viterbi</td>
<td>2069</td>
<td>2 459 801 548</td>
<td>68.67%</td>
</tr>
<tr>
<td>$A^*$ (1 Thread)</td>
<td>6134</td>
<td>283 041 383</td>
<td>70.01%</td>
</tr>
<tr>
<td>$A^*$ (4 Threads)</td>
<td>2497</td>
<td>283 041 383</td>
<td>70.01%</td>
</tr>
</tbody>
</table>

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3.2. Comparison with the Classical Viterbi

Table 1 shows the performance of our $A^*$ decoder compared to the classical Viterbi decoder. The experiment has been done with 32 Gaussian component distributions.

The main advantage of the Viterbi decoder comes from the fact that it computes only 29% of all likelihoods since they are computed on-demand. This allows the Viterbi decoder to perform very well in real time as shown by the results.

In the case of the $A^*$ decoder, results show that the sequential implementation is slower than the Viterbi decoder. This is mainly due to the acoustic likelihood computation which accounts for 64% of the total time. Recall that all likelihoods must be computed since they are needed for the heuristic. The heuristic computation itself accounts for 27% of the total time.

However, the 4 thread version, with a speed-up of 2.46, achieves real-time. This performance could be improved if more thread were available.

Note that the number of explored nodes is about 8.7 times smaller in the $A^*$ decoder. This is the reason why the search itself account for only 7% of the total computation time.

Figure 2 shows results of a second experiment ran with a 128 Gaussian component acoustic model distribution. In this scenario, the real-time accuracy of the Viterbi decoder drops to around 65%, even if only 16% of acoustic likelihoods are computed, search time has to be limited by a low beam value.

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![Fig. 1. $A^*$ search by block](image1)

![Fig. 2. 128 Gaussian components $A^*$ decoder accuracy vs execution time. Dashed lines are projections.](image2)

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The A* decoder cannot achieve real time with only 4 threads even with a speed-up of 3 times over its sequential counterpart. However, projection (represented by dashed lines) to 8 threads show that real-time can be reached with an accuracy of 71.62%. With 16 threads real-time accuracy would be 72.29%.

Note that for an accuracy of 72%, the A* decoder with 4 threads is 2.27 times faster than the Viterbi decoder. It would be 3.7 and 5.34 times faster with 8 and 16 threads.

### 3.3. Parallelization of Heuristic Computation

As described earlier, the heuristic computation operates in 2 steps: computation of acoustic likelihoods and computation of heuristic costs. These steps take more than 91% of the total search time. Table 2 shows how the computation time can be decreased by using multi-core architectures. Experiments have been conducted with 128 Gaussians acoustic models on the whole test set.

<table>
<thead>
<tr>
<th>Step</th>
<th>Computation time</th>
<th>speed-up factor</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1 thread</td>
<td>4 threads</td>
</tr>
<tr>
<td>Acoustic likelihoods</td>
<td>10659 sec</td>
<td>2913 sec</td>
</tr>
<tr>
<td>Heuristic costs</td>
<td>1512 sec</td>
<td>495 sec</td>
</tr>
</tbody>
</table>

Table 2. Heuristic computation speed-up.

The first line of Table 2 shows that computation of acoustic likelihoods parallelizes very well in a multicore processor with a speed-up approaching the theoretical maximum of N, where N is the number of cores.

Note that this parallelization could also be applied in the classical Viterbi decoder. However, the improvement will not be as significant since likelihoods are computed on-demand and only a subset of the distributions are used.

Heuristic costs are computed by applying the Viterbi algorithm on the reversed heuristic FST and starting from the last frame. Note that epsilon transition expansions, which take approximately 8.5% of the Viterbi computation time, are not parallelized.

We believe that the theoretical maximum is not being reached on this part because of a misuse of the memory architecture, and that an optimisation of the data structures will enhance performances on multicore processors.

### 5. REFERENCES


